Problem 75

(a) A person's blood pressure is measured to be $120 \pm 2 \text{ mm Hg}$. What is its percent uncertainty? (b) Assuming the same percent uncertainty, what is the uncertainty in a blood pressure measurement of 80 mm Hg?

Solution

Part (a)

Use the formula for percent uncertainty and plug in the numbers.

Percent Uncertainty =
$$\frac{\delta A}{A} \times 100\% = \frac{2 \text{ mm Hg}}{120 \text{ mm Hg}} \times 100\% \approx 2\%$$

Part (b)

Start with the same formula.

Percent Uncertainty =
$$\frac{\delta A}{A} \times 100\%$$

Assume that the percent uncertainty is the same as in part (a) and that the blood pressure is 80 mm Hg.

$$\frac{2 \text{ mm Hg}}{120 \text{ mm Hg}} \times 100\% = \frac{\delta A}{80 \text{ mm Hg}} \times 100\%$$

Solve for δA , the uncertainty.

$$\frac{2}{120} = \frac{\delta A}{80 \text{ mm Hg}}$$

Multiply both sides by 80 mm Hg.

$$\delta A = \frac{2(80)}{120} \text{ mm Hg} = \frac{4}{3} \text{ mm Hg} \approx 1 \text{ mm Hg}$$

Consequently,

Minimum Blood Pressure: 80 mm Hg
$$-\frac{4}{3}$$
 mm Hg \approx 79 mm Hg

Maximum Blood Pressure: 80 mm Hg +
$$\frac{4}{3}$$
 mm Hg ≈ 81 mm Hg.